

ARTICLE

Open Access

A novel scheme for ultrashort terahertz pulse generation over a gapless wide spectral range: Raman-resonance-enhanced four-wave mixing

Jiaming Le¹, Yudan Su², Chuanshan Tian^{1,3}✉, A. H. Kung¹ and Y. Ron Shen^{1,2}✉

Abstract

Ultrashort energetic terahertz (THz) pulses have created an exciting new area of research on light interactions with matter. For material studies in small laboratories, widely tunable femtosecond THz pulses with peak field strength close to MV cm^{-1} are desired. Currently, they can be largely acquired by optical rectification and difference frequency generation in crystals without inversion symmetry. We describe in this paper a novel scheme of THz pulse generation with no frequency tuning gap based on Raman-resonance-enhanced four-wave mixing in centrosymmetric media, particularly diamond. We show that we could generate highly stable, few-cycle pulses with near-Gaussian spatial and temporal profiles and carrier frequency tunable from 5 to >20 THz. They had a stable and controllable carrier-envelope phase and carried ~ 15 nJ energy per pulse at 10 THz (with a peak field strength of $\sim 1 \text{ MV cm}^{-1}$ at focus) from a 0.5-mm-thick diamond. The measured THz pulse characteristics agreed well with theoretical predictions. Other merits of the scheme are discussed, including the possibility of improving the THz output energy to a much higher level.

Introduction

The advent of intense ultrashort coherent light pulses has revolutionized the spectroscopy field^{1–3}. On one hand, they allow easy observation of various nonlinear optical effects and facilitate characterization of materials with nonlinear optical spectroscopy. On the other hand, they provide means for strong selective excitation of materials, and optical manipulation of material structure and properties such as optical-field-induced ferroelectricity, superconductivity, and others^{4–6}. They have also created the vibrant field of ultrafast dynamics of low-frequency excitations in materials¹. Thanks to advances in laser technology over the past decades, intense femtosecond (fs) pulses from table-top setups are now available over

essentially the whole spectral range from ~ 10 THz to soft X-ray even in ordinary laboratories. Below ~ 5 THz, high-intensity picosecond pulses exist⁷, but between 5 and 12 THz, stable, continuously tunable, energetic fs pulses are more difficult to come by^{8–10}. Yet this is a spectral range of great importance for materials studies. Phonons and vibrations of molecules and solids composed of heavier atoms are in this range, and so are the intermolecular (or inter-molecular-group) vibrations of molecular systems in chemistry and biology. Various elementary excitations of solids also lie in this spectral region. In the review article on “The 2017 Terahertz Science and Technology Roadmap”, the 5 to 15 THz spectral range was labeled as the present-day THz gap calling to be filled^{8,9}.

Currently, optical rectification (OR) or difference frequency generation (DFG) in second-order nonlinear crystals is the common technique to generate intense THz pulses. However, because of phonon absorption, THz generation from crystals is limited. For example, GaSe is among the few best nonlinear crystals for THz generation^{11–13}, but it has several absorption bands between

Correspondence: Chuanshan Tian (cstian@fudan.edu.cn) or Y. Ron Shen (yrshen@berkeley.edu)

¹Department of Physics, State Key Laboratory of Surface Physics and Key Laboratory of Micro- and Nano-Photonic Structure (MOE), Fudan University, Shanghai 200433, China

²Department of Physics, University of California, Berkeley, CA 94720, USA

Full list of author information is available at the end of the article

These authors contributed equally: Jiaming Le, Yudan Su

© The Author(s) 2023



Open Access This article is licensed under a Creative Commons Attribution 4.0 International License, which permits use, sharing, adaptation, distribution and reproduction in any medium or format, as long as you give appropriate credit to the original author(s) and the source, provide a link to the Creative Commons license, and indicate if changes were made. The images or other third party material in this article are included in the article's Creative Commons license, unless indicated otherwise in a credit line to the material. If material is not included in the article's Creative Commons license and your intended use is not permitted by statutory regulation or exceeds the permitted use, you will need to obtain permission directly from the copyright holder. To view a copy of this license, visit <http://creativecommons.org/licenses/by/4.0/>.

10 and 20 THz and a precipitous drop in transmission below 10 THz^{14,15}. The strong dispersion of the reststrahlen band at ~ 8 THz limits the effective coherent length of fs DFG in GaSe to ~ 200 μm in the 10–20 THz range (with pump wavelength around 1 μm) and distorts the THz temporal profile. The effective coherence length becomes much less than 100 μm below 10 THz. Organic nonlinear crystals have been used for efficient THz generation, but they have only a few narrow transparent windows above 5 THz and suffer from low optical damage thresholds¹⁶. Laser-induced gas plasmas can generate energetic THz pulses with spectra peaked at low THz and a broad wing extending to >50 THz. They are well suited as probes for linear THz spectroscopy over a wide spectral range, but their complex spatial mode patterns make them less desired as pumps for strong resonant excitations^{17–19}. Free electron lasers and electron-driven THz sources can also produce fs pulses covering the entire THz spectral range^{20,21}, but they are not readily available for most researchers. One may think four-wave mixing as a frequency conversion process could generate desirable THz pulses from materials if the input beams are sufficiently intense.

Indeed, THz generations by four-wave mixing²² and seeded optical Kerr amplification²³ in crystals were proposed earlier, but they ran into difficulties in practice. The third-order nonlinear susceptibilities of materials are small ($\chi^{(3)} \sim 10^{-14}$ to 10^{-15} esu or 10^{-22} to 10^{-23} $\text{m}^2 \text{V}^{-2}$). Generation of >10 nJ THz pulses requires input pulses with peak intensities higher than a few TW cm^{-2} , which is above the optical damage threshold of most materials. The scheme can be made practical only if $\chi^{(3)}$ of a material can be greatly enhanced through resonances while the optical damage threshold is still sufficiently high. This is

achievable in wide band gap materials with two of the inputs exciting a Raman resonance. Of these materials, diamond is most attractive because of its unique absorption spectrum (see Supplementary Information, SI, for more details).

Diamond has no intrinsic absorption throughout the spectral range from 0 to 5.5 eV ($44,000 \text{ cm}^{-1}$) except for some minor absorption between 1600 and 4000 cm^{-1} due to multi-phonon transitions. It possesses a nonresonant $\chi^{(3)}$ of $\sim 4.6 \times 10^{-14}$ esu ($6.4 \times 10^{-22} \text{ m}^2 \text{V}^{-2}$) that is resonantly enhanced to $\sim 6 \times 10^{-12}$ esu ($8 \times 10^{-20} \text{ m}^2 \text{V}^{-2}$) near the Raman resonance at 40 THz²⁴. The optical damage threshold of a typical CVD diamond plate is $\sim 7 \text{ TW cm}^{-2}$ for ~ 60 fs pulses at 50 THz in the infrared (measured value on our CVD diamond at 50 THz). With all three inputs in the infrared, noncollinear phase matching in four-wave mixing is possible from 2.5 to >100 THz. We report here a successful demonstration of THz generation by resonant four-wave mixing (R-FWM) in diamond. We were able to generate stable, few-cycle, transform-limited THz pulses that were tunable from 5 to >20 THz with controllable carrier-envelope phase (CEP) and had ≥ 10 nJ per pulse. This THz generator nicely covers the existing THz gap in THz spectroscopy^{8,9}. We summarize in Table 1 the data on THz pulse generation by different schemes commonly used in small laboratories for comparison.

Theory for THz generation by Raman-resonant four-wave mixing in diamond

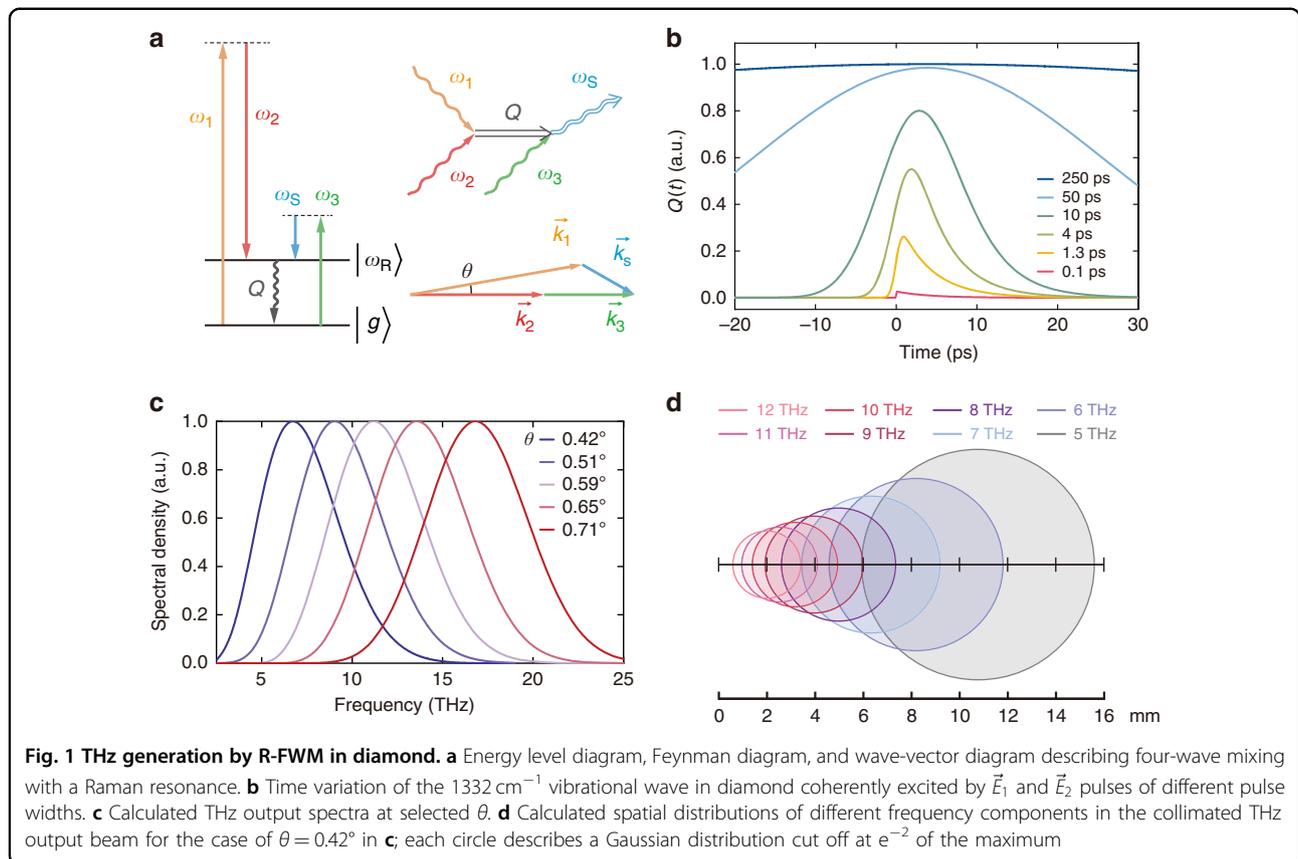
The basic theory behind resonant four-wave mixing (R-FWM) is straightforward. The three pulsed inputs, described by $\vec{E}_i(\omega_i, \vec{r}, t) = \vec{E}_i(\vec{r}, t) \exp(i\vec{k}_i \cdot \vec{r} - i\omega_i t)$ with

Table 1 Summary of THz generation schemes commonly used in small laboratories

Scheme	Reference	Input parameters		Output characteristics			
		Wave-length (μm)	Pulse energy (μJ)	Peak freq. (THz)	Bandwidth (THz)	Pulse energy (μJ)	Conversion (%)
OR in LiNbO ₃	Ref. 25	0.8	6.5×10^3	0.35	0.5	6.4	1
Gas plasma	Ref. 26	0.8	560	6	12	$\sim 0.06^a$	$\sim 0.1^a$
DFG in GaSe	Ref. 11	1.1	~ 300	30	10	1.7	~ 6
		~ 1.2	~ 300				
DFG in GaSe	Ref. 13	1.03	~ 3	13	6	$1.5 \times 10^{-3, b}$	0.5^b
		1.07	4.7				
R-FWM in diamond	This work	1.45	85	5	9	5×10^{-3}	0.5
		1.80	35	10		1.5×10^{-2}	1.5
		~ 6	10	15		4.1×10^{-2}	4

^aEstimated with 10^{-4} yield

^bScaled from THz generation at higher frequency in ref. 13. The pulse repetition rate was 190 kHz



center frequency ω_i ($i = 1, 2,$ and 3), induce a third-order nonlinear polarization $\vec{P}^{(3)}(\omega_S = \omega_3 - \omega_1 + \omega_2, \vec{r}, t)$ with center frequency at ω_S in a medium, where $\omega_1 - \omega_2 \sim \omega_R$ with ω_R being the Raman resonance frequency (Fig. 1a). Knowing $\vec{P}^{(3)}(\omega_S, \vec{r}, t)$, we can solve the wave equation to find the output field $\vec{E}_S(\omega_S, \vec{r}, t)$. For generation of fs THz pulses, however, a few details should be noted (see SI for details). The Raman linewidth of diamond is $\sim 1.25\text{ cm}^{-1}$, corresponding to a $\sim 4\text{ ps}$ vibrational dephasing time. This means that fs input pulses of \vec{E}_1 and \vec{E}_2 can only excite the Raman resonance weakly. To fully benefit from the Raman resonance enhancement of $\chi^{(3)}$, we must employ picosecond \vec{E}_1 and \vec{E}_2 pulses for excitation.

The R-FWM process can be understood as follows²⁷: The ps \vec{E}_1 and \vec{E}_2 input pulses coherently excite the transient vibrational wave, $\vec{Q}(\vec{r}, t)$, associated with the Raman resonance in diamond; the fs \vec{E}_3 input pulse then beats with the vibrational wave in diamond at a selected time to create the fs THz pulse. We can find $\vec{Q}(\vec{r}, t)$ from given $\vec{E}_1(\vec{r}, t)$ and $\vec{E}_2(\vec{r}, t)$ by solving the equation of motion for $\vec{Q}(\vec{r}, t)$. We can write $Q(t) \equiv f(t)Q_{st}$, where $Q_{st} \propto E_{1m}E_{2m}$ is the steady-state $Q(t)$ that would appear if $E_1(t)$ and $E_2(t)$ with peak values of E_{1m} and E_{2m} were long pulses. Beating of $\vec{E}_3(\vec{r}, t)$ and $\vec{Q}(\vec{r}, t)$ then induces $\vec{P}^{(3)}(\omega_S, \vec{r}, t) = \vec{\chi}_{res}^{(3)}(t) : \vec{E}_{1m}^*(\vec{r})\vec{E}_{2m}(\vec{r})\vec{E}_3(\vec{r}, t)$ with $\vec{\chi}_{res}^{(3)}(t) = f(t)(\vec{\chi}_{res}^{(3)})_{st}$. Plotted in

Fig. 1b is the calculated $Q(t)$ for diamond under Gaussian pulse excitation of $\vec{E}_1^*(t)\vec{E}_2(t)$ with different pulse widths. It is seen that for a pulse width of 1.3 ps, $Q(t)$ can reach a peak value of $\sim 30\%$ of Q_{st} in diamond with a corresponding $\vec{\chi}_{res}^3(t) \sim 0.3(\vec{\chi}_{res}^3)_{st}$.

With $\vec{P}^{(3)}(\omega_S, \vec{r}, t)$ known from given $\vec{E}_1(\vec{r}, t)$, $\vec{E}_2(\vec{r}, t)$ and $\vec{E}_3(\vec{r}, t)$, we can find the THz output by solving the wave equation or by numerically calculating the output field from the dipole radiation equation²⁸. Details of the calculations are presented in SI. For quantitative evaluation, we considered the case of 1.3 ps E_1 and E_2 pulses at 206 and 166 THz, respectively, to excite the Raman resonance of a 500- μm diamond (001) plate and a 60 fs E_3 pulse with center frequency tunable from 45 to 60 THz to generate 5 to 20 THz output; all beams were p-polarized along [110] and incident on diamond at $\sim 45^\circ$. The wave vector diagram sketched in Fig. 1a shows that noncollinear phase matching of the R-FWM process is possible. For each θ between \vec{k}_1 and $\vec{k}_2 \parallel \vec{k}_3$, there is a corresponding phase-matched (PM) THz output with a bandwidth of a few THz that satisfies the near-phase-matching condition of $\Delta kl/2 < 1$, where l is the beam path length in diamond²⁴. Thus, the transform-limited THz output should appear as fs pulses. The calculated THz output spectra for different θ are described in Fig. 1c. Because of the ω_S^2 dependence of THz generation, the peaks

of the spectra are blue shifted from those expected from PM. The near-PM requirement also leads to emission of different THz components in different directions with different angular spreads (see SI and Fig. S3). Collimation after the beam exit from diamond makes different THz components appear with differently displaced near-circular Gaussian distributions in the collimated beam. Figure 1d is an example showing the PM 5 THz distribution at the center and those of other frequency components away from the center. Focusing of the collimated beam or imaging of the beam exit from diamond recombined all the THz frequency components at the image position.

For a crude estimate on the THz output, we can use the usual expression for output energy per pulse from wave mixing under the pump-depletion-less limit. The energy per pulse for THz generation from phase-matched four wave mixing is given by:

$$W(\omega_s) \sim \frac{16\pi^4 \omega_s^2}{c^4 n_1 n_2 n_3 n_s} |\chi^{(3)} l|^2 \frac{W(\omega_1) W(\omega_2)}{A^2 T^2} W(\omega_3)$$

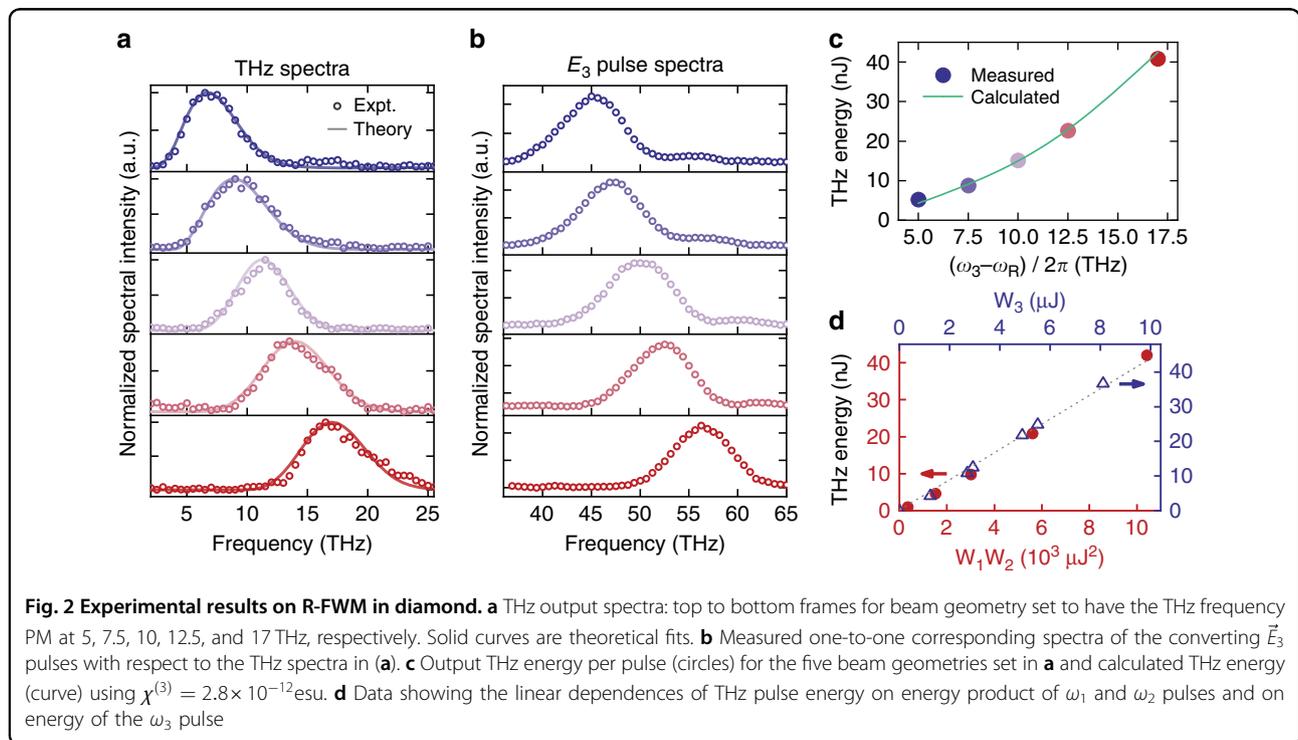
in cgs units, where A is the beam overlapping area, T is the pulse width of \vec{E}_1 and \vec{E}_2 , and l is the interacting path length. For the diamond case, if we take $|\chi^{(3)}| = 0.3|\chi_{\text{res}}^{(3)}|_{\text{st}} \sim 2 \times 10^{-12} \text{esu}$ ($\sim 3 \times 10^{-20} \text{m}^2 \text{V}^{-2}$), $l = 0.5 \text{mm}$, $W(\omega_1) = W(\omega_2) = 40 \mu\text{J}$, $W(\omega_3) = 10 \mu\text{J}$, $A = 4 \times 10^{-4} \text{cm}^2$, and $T = 1.3 \text{ps}$, we find $W(\omega_s) \sim 14 \text{nJ}$ per pulse at $\omega_s/2\pi = 10 \text{THz}$ with a pulse width nearly the same as that of the \vec{E}_3 input. This suggests that R-FWM in diamond can be a powerful THz generator.

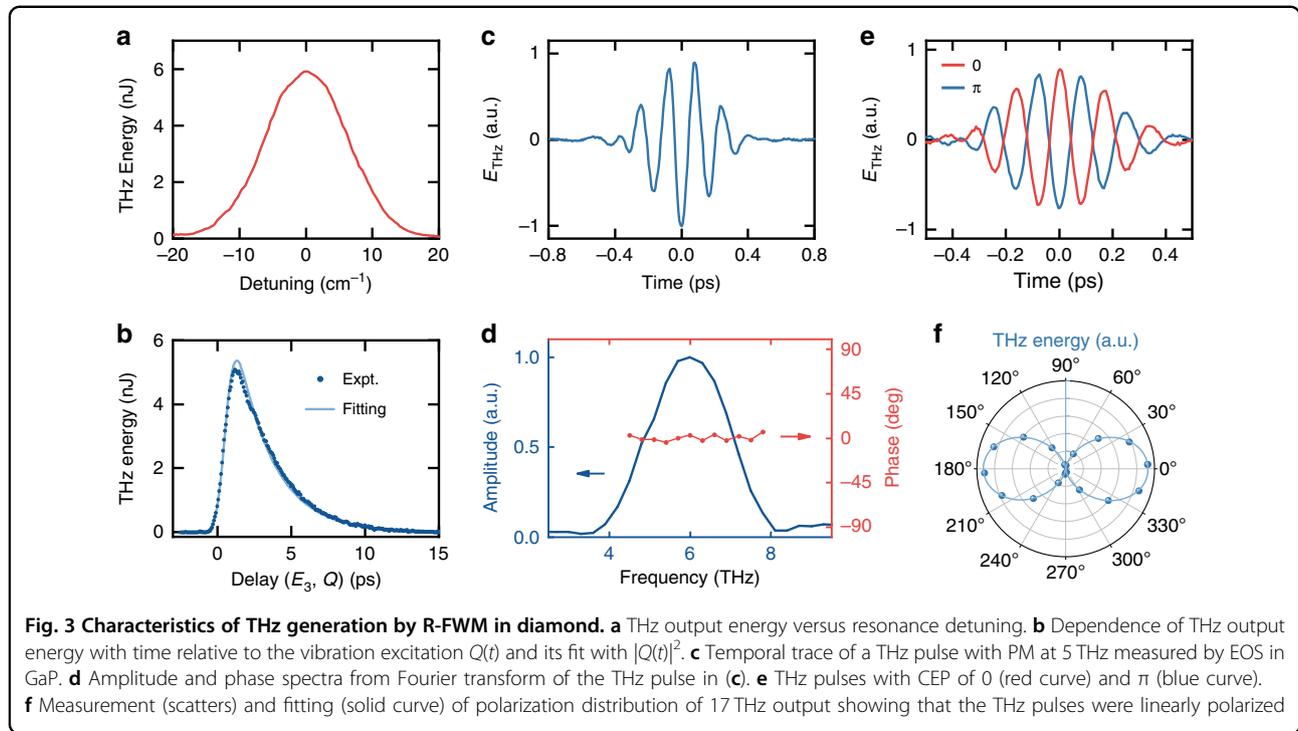
Experimental arrangement

In the experiment, we used a commercial 33-fs, 5-W, 1-kHz Ti:sapphire laser system to pump two optical parametric amplifiers (OPA) seeded by a common white light source. (Details of the experimental arrangement is given in SI). The signal and idler from OPA-1 centered at $\omega_1/2\pi = 206 \text{THz}$ and $\omega_2/2\pi = 166 \text{THz}$ were stretched to 1.3-ps positively chirped pulses with a constant instantaneous difference frequency of 40 THz. The ω_3 pulses of 63-fs width, tunable between 40 and 60 THz were derived from OPA-2 with a difference frequency generation stage. All three p-polarized pulses were incident on a 0.5-mm (001)-cut diamond plate at $\sim 45^\circ$ and overlapped over an area inside diamond of $\pi(140 \times 100)/2 \mu\text{m}^2$. The p-polarized THz outputs were characterized by knife-edge beam profiling, a Fourier transform infrared interferometer (FTIR) and electro-optic sampling (EOS) (see SI for details).

Results

Figure 2a shows a set of measured THz spectra generated by R-FWM with the beam geometry set to have θ at $0.42^\circ, 0.51^\circ, 0.59^\circ, 0.65^\circ$, and 0.71° . The input energies per pulse were $W_1 \approx 85 \mu\text{J}$, $W_2 \approx 35 \mu\text{J}$ and $W_3 \approx 10 \mu\text{J}$ on the overlapping area. The corresponding spectra of the ω_3 input pulses generating the THz spectra are given in Fig. 2b. It is seen that the two sets of spectra are very similar as expected except for an overall shift of 40 THz and some deviation due to the ω_s^2 dependence of THz generation. The measured THz spectra can be well fit by





theory as described in Fig. 2a. The total THz energy versus the THz frequency $\omega_3 - \omega_R$ is plotted in Fig. 2c. It is 5 nJ per pulse at 5 THz and increases to 41 nJ per pulse at 17 THz. In Fig. 2d, the output energy, $W(\omega_s)$, is seen to be linearly proportional to the input energies, $W_1 W_2$ and W_3 , as it should be. From the measured THz energies, we were able to deduce $|\chi_{res}^{(3)}|_{st} \sim 9 \times 10^{-12}$ esu ($\sim 1 \times 10^{-19}$ m² V⁻²), compared to 6×10^{-12} esu in ref. ²⁴ We also used a slit of variable width placed at various positions in the output beam to map out the spatial distribution of the THz output spectrum and found good agreement with theoretical prediction (see SI and Fig. S6). As expected, the THz output was spatially chirped (see Fig. 1d). With a pair of parabolic mirrors, the THz output re-focused at the image point appeared as transformed-limited fs pulses (see SI and Fig. S7). An appropriate aperture in the THz beam path could select a specific portion of the THz output to yield a THz pulse with the desired spectral and temporal profiles.

Figure 3a provides a description on the effect of detuning of excitation from Raman resonance. As $\omega_1 - \omega_2$ moves away from the resonance, the observed THz output drops as predicted. In another measurement, the overlapping time of the fs E_3 pulse with the excited vibration, $Q(t)$, was varied, the THz output went through a peak and then decayed, mapping out the variation of $Q(t)$, as depicted in Fig. 3b. Theoretical fit of the data allowed the deduction of the phonon dephasing time, $T_2 = 4.8$ ps.

We also characterized the THz output in the time domain by EOS. The result for a THz output pulse PM at 5 THz is displayed in Fig. 3c with its Fourier-transformed amplitude and phase spectra in Fig. 3d. Due to absorption at higher THz frequencies in the EOS crystal, the EOS temporal trace was distorted into a broader pulse and a corresponding narrower FT spectrum compared to that measured directly by FTIR. The observed uniform spectra phase in Fig. 3d however implies that the THz pulse should be nearly transform-limited with a pulse width of ~ 70 fs. If such a pulse is focused to an area of $\sim (100 \mu\text{m})^2$, the peak electric field of 10 and 17 THz pulses with energy of 15 nJ and 41 nJ can reach about 1 and 1.7 MV cm⁻¹, respectively. The THz pulses were CEP locked, and the phase could be controllably changed by varying the time delay of the ω_3 pulse (see SI). Figure 3e shows two measured THz pulses with CEP adjusted to 0 and π ; a time delay of 13 fs of the ω_3 pulse led to a CEP change of π . The THz output generated was linearly polarized in the same plane as the inputs as described in Fig. 3f.

Discussion

The above results constitute the first demonstration that R-FWM in centrosymmetric condensed media can be effective to generate energetic THz pulses. Diamond, in particular, has attractive merits. Its high optical damage threshold allows input pump intensities to be so high as to induce third-order nonlinear optical effects (e.g., FWM) competing with second-order effects

(e.g., DFG) in other crystals. Transparency throughout the region from THz to UV leads to weak frequency dispersion of optical response coefficients that facilitates phase-matched THz pulse generation over a very wide spectral range with exceptionally good quality. With the phonon mode Raman-excited by ps pulses, the coherent phonon wave hardly changes on the fs time scale. It is then seen that R-FWM for fs THz pulse generation in diamond is effectively a beating process between a fs IR pulse with a constant phonon wave or a frequency conversion process down-converting the fs IR pulse by the phonon wave to the fs THz pulse. The latter essentially duplicates the input fs IR pulse except for a shift in frequency and some modification due to radiation efficiency. Thus, the characteristics of the THz pulse can be readily tuned by tuning the corresponding characteristics of the input IR pulse. The energy conversion efficiency is given directly by the ratio of the output THz pulse energy to the input fs pulse energy. We have measured phase-matched THz pulse generation with the center frequency spanning from 5 to 20 THz, but this spectral range can be readily extended to >100 THz. As the THz radiation efficiency increases with square of the frequency, and there is more pulse energy at higher input frequency, we expect the output energy at higher THz frequency generated by R-FWM in diamond can reach a level comparable to that generated by DFG in GaSe or other crystalline compounds.

As a first demonstration of THz generation by R-FWM, we have not optimized the parameters in our experiment. We can increase the peak intensities of the three input pulses on diamond by an overall factor of 10 before reaching the optical damage threshold. Doubling the diamond thickness would increase the conversion efficiency by ~ 4 . If more input energy from the laser system is available to pump a larger area of diamond, the THz output energy can be further improved in proportional to the beam area. While the R-FWM scheme is more complex in experimental arrangement, it has obvious merits compared to the other schemes listed in Table 1, namely, the wide tunability of the center frequency and band width of the fs THz pulses, their near-Gaussian spatial and temporal profiles, and the relatively high conversion efficiency from IR input to THz output.

Summary and prospects

Our study has unequivocally established that R-FWM in diamond can be made into a high-quality, powerful, fs THz generator over a wide spectral range without any gap. For fs THz pulse generation, R-FWM in diamond can be regarded as a direct frequency down-conversion process that converts a fs input pulse at higher frequency to a fs THz pulse that has characteristics essentially

duplicating the characteristics of the input pulse except for the frequency shift. An input pulse of high quality, in terms of spatial, spectral, and temporal profiles as well as amplitude and phase stability, generates a THz pulse of nearly equal high quality. Tuning the characteristics of the input pulse tunes the characteristics of the THz output pulse accordingly. In this respect, we can amplitude- or polarization-modulate the THz pulse simply by modulating the input pulse²⁹.

With a fs commercial laser system, we were able to use R-FWM in diamond to generate stable fs THz pulses over a wide spectral range with very high quality. The THz output energy was >10 nJ (producing a peak field strength $\sim 1 \text{ MV cm}^{-1}$ at a 100- μm focal spot) at 10 THz, and higher for higher THz frequencies. It could be enhanced by at least one order of magnitude with a higher input pulse energy and a thicker diamond plate. We also note that R-FWM in diamond can be collinearly phase-matched if the diamond plate is made birefringent by uniaxial stress of $\sim 1 \text{ GPa}$. Growth of CVD diamond to >6 mm thick was recently reported³⁰; collinear PM in such a diamond plate would push R-FWM toward the pump depletion region and a THz output of >1 μJ per pulse should be easily attainable with an input of $\sim 10 \mu\text{J}$ per pulse from the converting pulses, corresponding to a peak THz field strength of a 50 fs THz pulse to >10 MV cm^{-1} if focused to an area of $\sim (100 \mu\text{m})^2$.

Acknowledgements

Our thanks are due to Ya Cheng (East China Normal University) for his help on pulse stretcher, Chih-Hsuan Lu and Jhan-Yo Guo (Tsing Hua University) for their assistance on the experimental setup, and Chao-Nan Lin and Chong-Xin Shan (Zhengzhou University) for providing CVD diamond plates. This work was supported by the National Natural Science Foundation of China Grants (No. 12125403 and No. 11874123) and the National Key Research and Development Program of China (No. 2021YFA1400503 and No. 2021YFA1400202).

Author details

¹Department of Physics, State Key Laboratory of Surface Physics and Key Laboratory of Micro- and Nano-Photonic Structure (MOE), Fudan University, Shanghai 200433, China. ²Department of Physics, University of California, Berkeley, CA 94720, USA. ³Collaborative Innovation Center of Advanced Microstructures, Nanjing 210093, China

Author contributions

Y.R.S. conceived the idea. Y.R.S., A.H.K., J.L., and Y.S. designed the experiment. J.L. and Y.S. developed the theoretical framework, performed the calculation, conducted the experiment, and analyzed the data with guidance from Y.R.S. and A.H.K. All authors participated in discussions over research progresses. Y.R.S., Y.S., and J.L. wrote the paper with input from all authors. C.T. supervised and managed the project, secured funding, and carried general responsibility.

Data availability

All data are available in the main text or the supplementary materials.

Conflict of interest

The authors declare no competing interests.

Supplementary information The online version contains supplementary material available at <https://doi.org/10.1038/s41377-023-01071-z>.

Received: 5 December 2022 Revised: 28 December 2022 Accepted: 3 January 2023

Published online: 02 February 2023

References

1. Kruchinin, S. Y., Krausz, F. & Yakovlev, V. S. *Colloquium: strong-field phenomena in periodic systems*. *Rev. Mod. Phys.* **90**, 021002 (2018).
2. Disa, A. S., Nova, T. F. & Cavalleri, A. Engineering crystal structures with light. *Nat. Phys.* **17**, 1087–1092 (2021).
3. Bao, C. et al. Light-induced emergent phenomena in 2D materials and topological materials. *Nat. Rev. Phys.* **4**, 33–48 (2022).
4. Nova, T. F. et al. Metastable ferroelectricity in optically strained SrTiO₃. *Science* **364**, 1075–1079 (2019).
5. Li, X. et al. Terahertz field-induced ferroelectricity in quantum paraelectric SrTiO₃. *Science* **364**, 1079–1082 (2019).
6. Nicoletti, D. et al. Magnetic-field tuning of light-induced superconductivity in striped La_{2-x}Ba_xCuO₄. *Phys. Rev. Lett.* **121**, 267003 (2018).
7. Hirori, H. et al. Single-cycle terahertz pulses with amplitudes exceeding 1 MV/cm generated by optical rectification in LiNbO₃. *Appl. Phys. Lett.* **98**, 091106 (2011).
8. Dhillon, S. S. et al. The 2017 terahertz science and technology roadmap. *J. Phys. D: Appl. Phys.* **50**, 043001 (2017).
9. Salén, P. et al. Matter manipulation with extreme terahertz light: progress in the enabling THz technology. *Phys. Rep.* **836-837**, 1–74 (2019).
10. Zhang, X. C., Shkurinov, A. & Zhang, Y. Extreme terahertz science. *Nat. Photon.* **11**, 16–18 (2017).
11. Sell, A., Leitenstorfer, A. & Huber, R. Phase-locked generation and field-resolved detection of widely tunable terahertz pulses with amplitudes exceeding 100 MV/cm. *Opt. Lett.* **33**, 2767–2769 (2008).
12. Junginger, F. et al. Single-cycle multiterahertz transients with peak fields above 10 MV/cm. *Opt. Lett.* **35**, 2645–2647 (2010).
13. Knorr, M. et al. Phase-locked multi-terahertz electric fields exceeding 13 MV/cm at a 190 kHz repetition rate. *Opt. Lett.* **42**, 4367–4370 (2017).
14. Giorgianni, U. et al. Infrared and UV-visible spectra of layer semiconductors GaS, GaSe and GaTe. *J. Phys.* **38**, 1293–1299 (1977).
15. Guo, J. et al. Doped GaSe crystals for laser frequency conversion. *Light Sci. Appl.* **4**, e362 (2015).
16. Liu, B. et al. Generation of narrowband, high-intensity, carrier-envelope phase-stable pulses tunable between 4 and 18 THz. *Opt. Lett.* **42**, 129–131 (2017).
17. Andreeva, V. A. et al. Ultrabroad terahertz spectrum generation from an air-based filament plasma. *Phys. Rev. Lett.* **116**, 063902 (2016).
18. You, Y. S., Oh, T. I. & Kim, K. Y. Off-axis phase-matched terahertz emission from two-color laser-induced plasma filaments. *Phys. Rev. Lett.* **109**, 183902 (2012).
19. Oh, T. I. et al. Intense terahertz generation in two-color laser filamentation: energy scaling with terawatt laser systems. *New J. Phys.* **15**, 075002 (2013).
20. Jeong, Y. U. et al. Prospects of a terahertz free-electron laser for field application. *J. Korean Phys. Soc.* **80**, 367–376 (2022).
21. Zhu, J. F. et al. Free-electron-driven multi-frequency terahertz radiation on a super-grating structure. *IEEE Access* **7**, 181184–181190 (2019).
22. Cook, D. J. & Hochstrasser, R. M. Intense terahertz pulses by four-wave rectification in air. *Opt. Lett.* **25**, 1210–1212 (2000).
23. Vampa, G. et al. Light amplification by seeded Kerr instability. *Science* **359**, 673–675 (2018).
24. Levenson, M. D. & Bloembergen, N. Dispersion of the nonlinear optical susceptibility tensor in centrosymmetric media. *Phys. Rev. B* **10**, 4447–4463 (1974).
25. Wu, X. J. et al. Terahertz generation in lithium niobate driven by Ti: sapphire laser pulses and its limitations. *Opt. Lett.* **39**, 5403–5406 (2014).
26. Ho, I. C., Guo, X. Y. & Zhang, X. C. Design and performance of reflective terahertz air-biased-coherent-detection for time-domain spectroscopy. *Opt. Express* **18**, 2872–2883 (2010).
27. Shen, Y. R. *The Principles of Nonlinear Optics* (J. Wiley, 1984).
28. Morris, J. R. & Shen, Y. R. Theory of far-infrared generation by optical mixing. *Phys. Rev. A* **15**, 1143–1156 (1977).
29. Sato, M. et al. Terahertz polarization pulse shaping with arbitrary field control. *Nat. Photon.* **7**, 724–731 (2013).
30. Lu, Y. J., Lin, C. N. & Shan, C. X. Optoelectronic diamond: growth, properties, and photodetection applications. *Adv. Opt. Mater.* **6**, 1800359 (2018).